

PH112

Quiz 5 Review

Review Session 2/27/19

Chapter 7: Work and Kinetic Energy

$$W = F \cdot \Delta x$$

$$= F \cdot dx$$

$$= F \cos(\theta) \cdot x$$

$$= \int F(x) dx$$

= area under F-x curve

$$= \Delta K \quad (\text{for chapter 7 perspective, no } U)$$

$$= \Delta E_{\text{total}} \quad (\text{external work on system for chapter 8 perspective})$$

$$= -dU \quad (\text{if } E_{\text{mec}} \text{ is conserved})$$

$$= \Sigma W$$

$$W_g = -mg\Delta h = \text{integral of } -mg$$

$$W_k = -1/2kx^2 = \text{integral of } -kx$$

$$K = 1/2mv^2$$

$$P = dW/dt$$

$$= F \cdot v$$

Chapter 8: Potential Energy

$$U = -F \cdot dx$$

= negative of work done by a force to get to a particular configuration

$$U_g = mgh$$

$$U_s = 1/2kx^2$$

Force is conservative if total work along a closed path is 0; these are path-independent

- Else nonconservative

Energy is always conserved

- Mechanical energy is not always conserved, but when it is then $E_{\text{mec}_2} = E_{\text{mec}_1}$

$$E_{\text{mec}} = U + K$$

$\Delta E_{\text{mec}} = \Delta U + W$ (here work is an "internal work" equal to ΔK , not work done on the system)

- if E_{mec} conserved, $\Delta U = -W$

$$\text{- then } dU = -W = -Fdx \Rightarrow F = -dU/dx$$

- useful b/c intermediate states do not have to be considered

- conservation of E_{mec} if no deformation of material, heat loss, (kinetic) friction

$$E_{\text{total}} = E_{\text{mec}} + E_{\text{th}} + E_{\text{int}}$$

$$\Delta E_{\text{total}} = \Delta E_{\text{mec}} + \Delta E_{\text{th}} + \Delta E_{\text{int}} \quad (\text{most general form})$$

- pretty much ignore E_{int} , E_{th} is applicable if there is friction/heat

- potential energy diagrams

- turning points and equilibrium points (neutral, stable, unstable)

$$W = \Delta E_{\text{total}} \quad (\text{work done on the system})$$

Chapter 9: Linear momentum & COM

$$\text{COM} = 1/M \cdot \int r dm$$

- or, for constant density: $\text{COM} = 1/P \cdot \int r dP$

Choose a good reference pt for COM for easy calculation

Take advantage of symmetries (spherical, linear)

$$F_{\text{net}} = M \cdot a_{\text{com}}$$

$$= dp/dv$$

- Net force can be thought of as concentrated at center of mass -- internal forces have no effect

$$p = M * v_{com} \quad (\text{momentum of system})$$

$$J = \int F(t) dt \quad (\text{impulse on system})$$

$$= \Delta p$$

Make sure to think about when energy and linear momentum are conserved. They are not mutually inclusive/exclusive!

- If both are conserved, you may need to end up using both

- If only one is conserved, make sure you do not use the wrong one.

Problems from class

Set up center of mass of two sticks

Spring and a dome question

Rockets

Two boats w/ coal

Boat with dog and person on both ends, switch sides

Conveyor belt

Ballistic pendulum